

Homework assignment #1 problems 2.5, 2.6, 2.8 from the book p. 15
and also the following two problems.

A How many $(n, 2, n)_3$ -codes are there?

How many $(n, 2, n)_q$ -codes are there?

B What is the smallest possible n for which an $(n, 4, 3)_2$ -code exists?
Find such a code of length n . To show that n is as small
as possible you must show that no $(m, 4, 3)_2$ -codes exist for all
 $m < n$.

C A symmetric communication channel for the binary alphabet
 $\{0, 1\}$ with $p(0|0) = p(1|1) = .95$ and $p(0|1) = p(1|0) = .05$.

Now suppose we are transmitting a code word of length 15.

What is the probability that the received word has
at most a 1-bit error?

Assignment #2

Problems from textbook 3.2, 3.6, 3.11, 3.16(i), 3.20, 3.23 cdef

Exam 1 covers chapters 1, 2, 3 and $\frac{1}{2}$ of Chapter 4.

At the earliest this will be on Monday Feb 6.

Note For two independent probabilities $p(O_1)$ and $p(O_2)$ The

$$\text{probability } p(O_1 \text{ and } O_2) = p(O_1)p(O_2)$$

when outcomes O_1 and O_2 mutually exclusive (cannot both occur)

$$p(O_1 \text{ or } O_2) = p(O_1) + p(O_2)$$

probability that
a 15-bit string
transmitted with
0 errors

$$= (.95)^{15} = .4632$$

probability that
a 15-bit string
transmitted with
one error at
bit $j \in \{1, \dots, 15\}$

$$= \binom{15}{1} (.95)^{14} (.05) = .0244$$

Probability that
a 15-bit string
transmitted with
at most 1 error

$$= .4632 + 15(.0244) = .8292 = \boxed{82.92\%}$$