

Written assignments
to hand in.

Section 3.2

26, 38

due Monday 11/13

Section 3.3

12, 58

due Tuesday 11/14

Section 3.5

24, 32

due Wednesday 11/15

Section 3.3

$$\textcircled{23} \quad \frac{x^6 + x^4 + x^2 + 1}{x^2 + 1}$$

$$= x^4 + 1$$

Discussion Problems
From the department syllabus
These are not to hand in.

Section 3.2,

3.3: 15-23 odd, 41-47 odd

WebAssign

3.1+3.2 Sunday 11/12 9pm

$$\begin{array}{r} x^4 + 1 \\ x^2 + 1 \overline{) x^6 + x^4 + x^2 + 1} \\ \underline{-(x^6 + x^4)} \\ x^2 + 1 \\ \underline{-(x^2 + 1)} \\ 0 \end{array}$$

(20)

$$\begin{array}{r}
 x^2 + 2x + 9 \\
 x^2 - 5x + 1 \overline{) x^4 - 3x^3 + x - 2} \\
 \underline{-(x^4 - 5x^3 + x^2)} \\
 2x^3 - x^2 + x - 2 \leftarrow \text{first remainder, deg} = 3 \\
 \underline{-(2x^3 - 10x^2 + 2x)} \\
 9x^2 - x - 2 \leftarrow 2^{\text{nd}} \text{ remainder deg} = 2 \\
 \underline{-(9x^2 - 45x + 9)} \\
 44x - 11 \leftarrow \text{Final remainder deg} = 1 < 2
 \end{array}$$

$$\frac{x^4 - 3x^3 + x - 2}{x^2 - 5x + 1} = x^2 + 2x + 9 + \frac{44x - 11}{x^2 - 5x + 1}$$

(59) $P(x) = x^3 - x^2 - 11x + 15$ confirm that $c=3$ is a root of $P(x)$. in other words, $P(3) = 0$.

$$P(3) = 27 - 9 - 33 + 15 = 0$$

By The Factor Theorem we know that

$x-3$ divides $P(x)$ evenly.

$$\begin{array}{r}
 x^2 + 2x - 5 \\
 x-3 \overline{) x^3 - x^2 - 11x + 15} \\
 \underline{-(x^3 - 3x^2)} \\
 2x^2 - 11x + 15 \\
 \underline{-(2x^2 - 6x)} \\
 -5x + 15 \\
 \underline{-(-5x + 15)} \\
 0
 \end{array}$$

Therefore $P(x) = x^3 - x^2 - 1(x + 15)$
 $= (x-3)(x^2 + 2x - 5)$ ← doesn't factor further.

quadratic formula for $x^2 + 2x - 5$ $x = \frac{-2 \pm \sqrt{4 + 20}}{2} = \frac{-2 \pm \sqrt{24}}{2}$
 $= \frac{-2 \pm 2\sqrt{6}}{2} = -1 \pm \sqrt{6}$

roots of $P(x)$ are $\boxed{x=3, -1+\sqrt{6}, -1-\sqrt{6}}$